

# Topic 10

## Amplification and Amplifiers

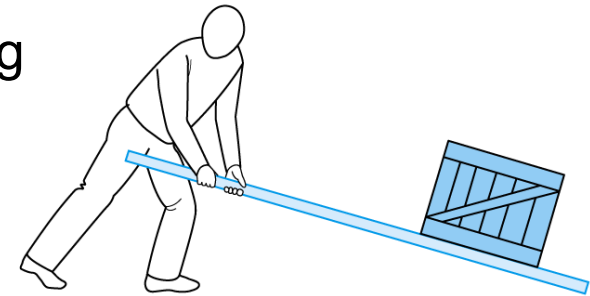
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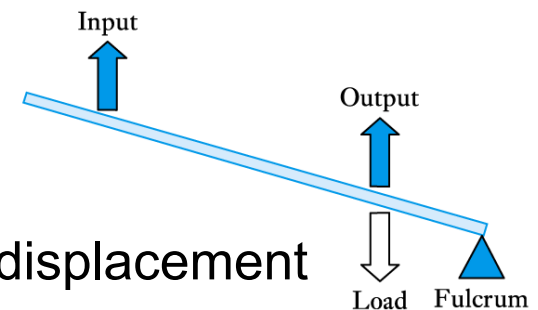
# The Idea of amplification

- ◆ Amplification is one of the most common processing functions
- ◆ **Amplification** means making things bigger
- ◆ **Attenuation** means making things smaller
- ◆ There are many non-electronic forms of amplification



- ◆ **Non-electronic amplifiers: Levers**

- Example shown on the right is a force *amplifier*, but a displacement *attenuator*
- Reversing the position of the input and output would produce a force *attenuator* but a displacement *amplifier*
- This is an example of a **non-inverting amplifier** (since the input and output are in the same direction)

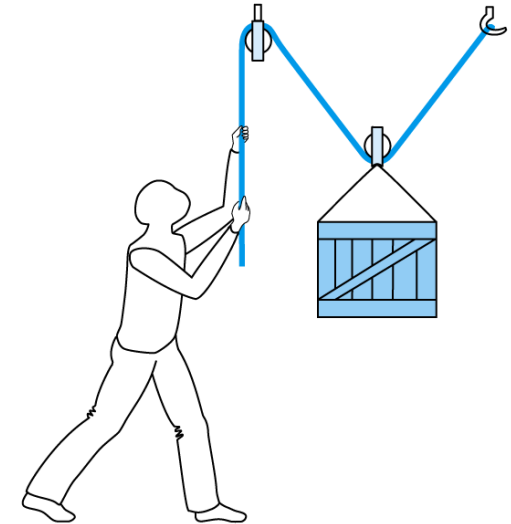


# Another example of amplification

## ◆ Non-electronic amplifiers

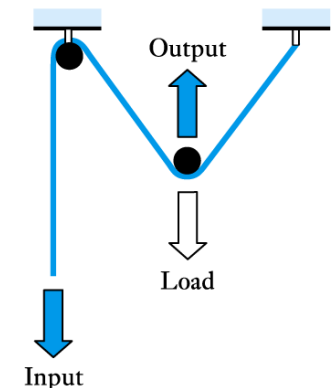
### – Pulleys

- Example shown here is a force *amplifier*, but a displacement *attenuator*
- This is an example of an **inverting amplifier** (since the input and output displacements are in opposite directions) but other pulley arrangements can be non-inverting



## ◆ Passive and active amplifiers

- Levers and pulleys are examples of **passive amplifiers** since they have no external energy source
  - In such amplifiers the power delivered at the output must be less than (or equal to) that absorbed at the input
- Some amplifiers are not passive but are **active amplifiers** in that they have an external source of power
  - In such amplifiers the output can deliver more power than is absorbed at the input



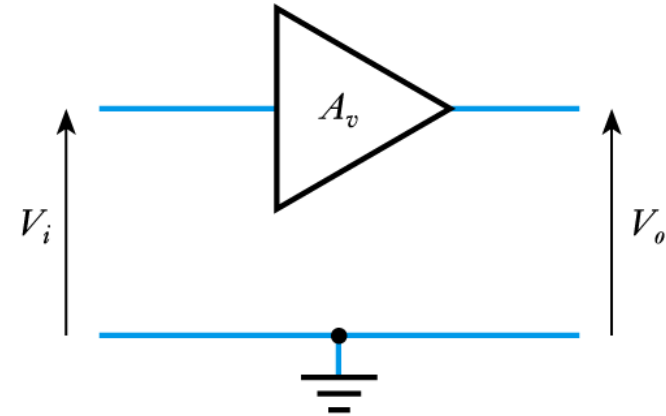
# Electronic Amplifiers

- ◆ We will concentrate on *active* electronic amplifiers
  - take power from a power supply
  - amplification described by gain

$$\text{Voltage Gain } (A_v) = \frac{V_o}{V_i} \text{ or } 20 \log_{10} \frac{V_o}{V_i} \text{ dB}$$

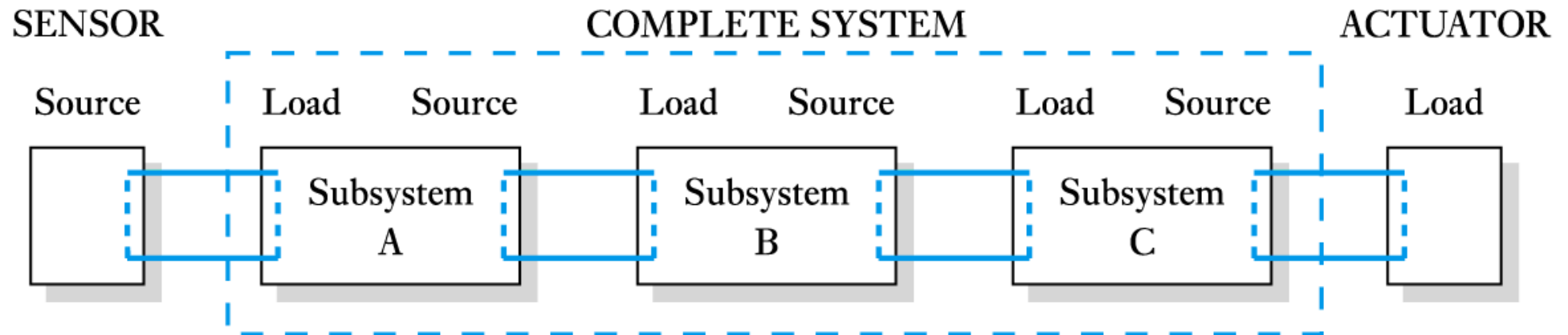
$$\text{Current Gain } (A_i) = \frac{I_o}{I_i} \text{ or } 20 \log_{10} \frac{I_o}{I_i} \text{ dB}$$

$$\text{Power Gain } (A_p) = \frac{P_o}{P_i} \text{ or } 10 \log_{10} \frac{P_o}{P_i} \text{ dB}$$



# Sources and Loads

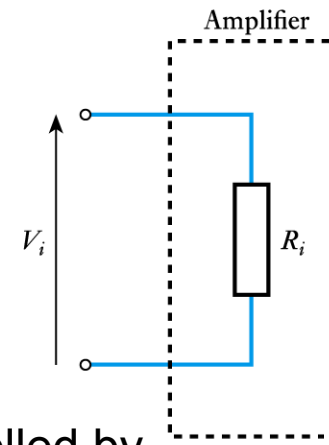
- ◆ An *ideal* voltage amplifier would produce an output determined only by the input voltage and its gain.
  - irrespective of the nature of the source and the load
  - in real amplifiers this is not the case
  - the output voltage is affected by **loading**



# Modelling Sources and Loads

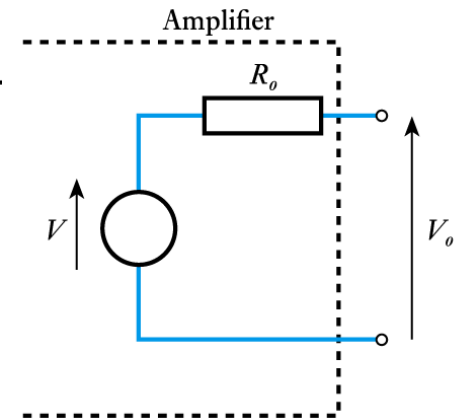
## ◆ Modelling the input of an amplifier

- the input can often be adequately modelled by a simple resistor
- the **input resistance**



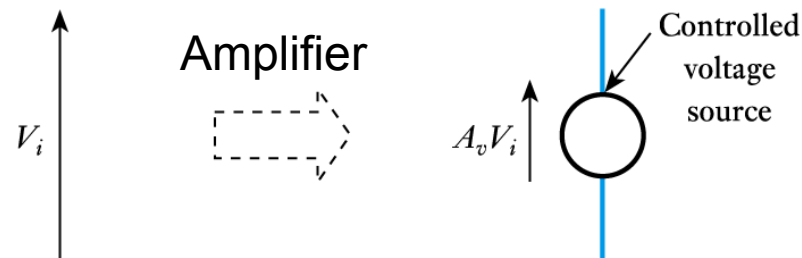
## ◆ Modelling the output of an amplifier

- Similarly, the output of an amplifier can be modelled by an ideal voltage source and an output resistance.
- This is an example of a **Thévenin equivalent circuit**



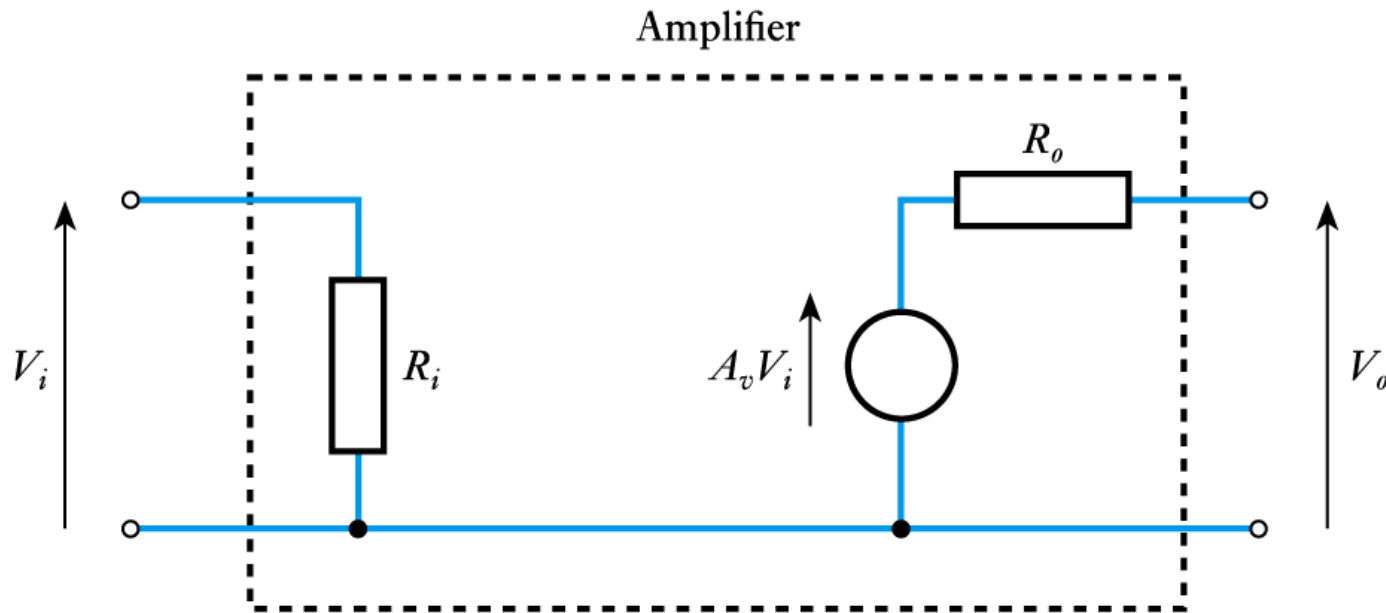
## ◆ Modelling the gain of an amplifier

- can be modelled by a controlled voltage source
- the voltage produced by the source is determined by the input voltage to the circuit



# Equivalent circuit of an amplifier

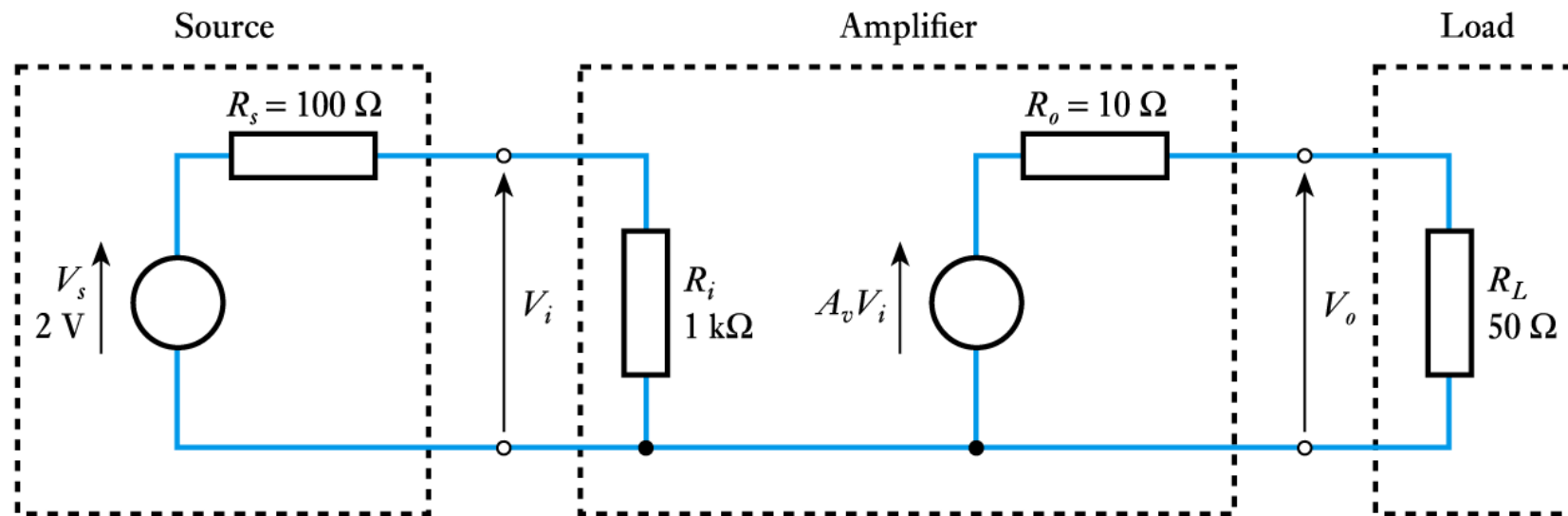
- ◆ We can put together the models for input, output and gain, to form a model of the entire amplifier as shown here



# An example (1)

- ◆ An amplifier has a voltage gain of 10, an input resistance of 1 k $\Omega$  and an output resistance of 10  $\Omega$ .
- ◆ The amplifier is connected to a sensor that produces a voltage of 2 V and has an output resistance of 100  $\Omega$ , and to a load of 50  $\Omega$ .
- ◆ What will be the output voltage of the amplifier (that is, the voltage across the load resistance)?

- ◆ We start by constructing an equivalent circuit of the amplifier, the source and the load:



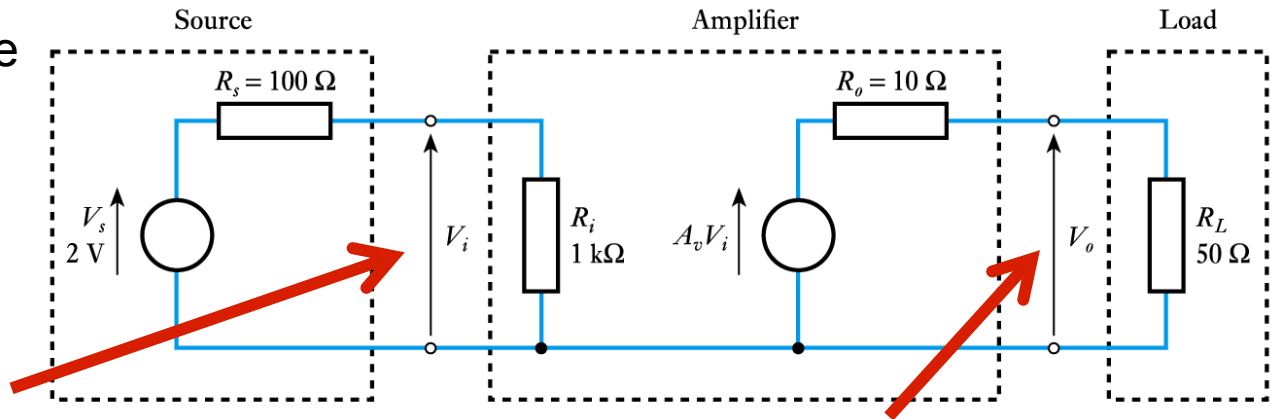


## An example (2)

- ◆ From this we calculate the output voltage:

$$V_i = \frac{R_i}{R_s + R_i} V_s$$

$$= \frac{1 \text{ k}\Omega}{100 \Omega + 1 \text{ k}\Omega} \times 2 \text{ V} = 1.82 \text{ V}$$



- ◆ Although the amplifier has a gain of 10 when it is NOT connected to anything, when used in the system, the actual gain is:

$$\text{Voltage Gain } (A_v) = \frac{V_o}{V_i} = \frac{15.2}{1.82} = 8.35$$

$$V_o = A_v V_i \frac{R_L}{R_o + R_L}$$

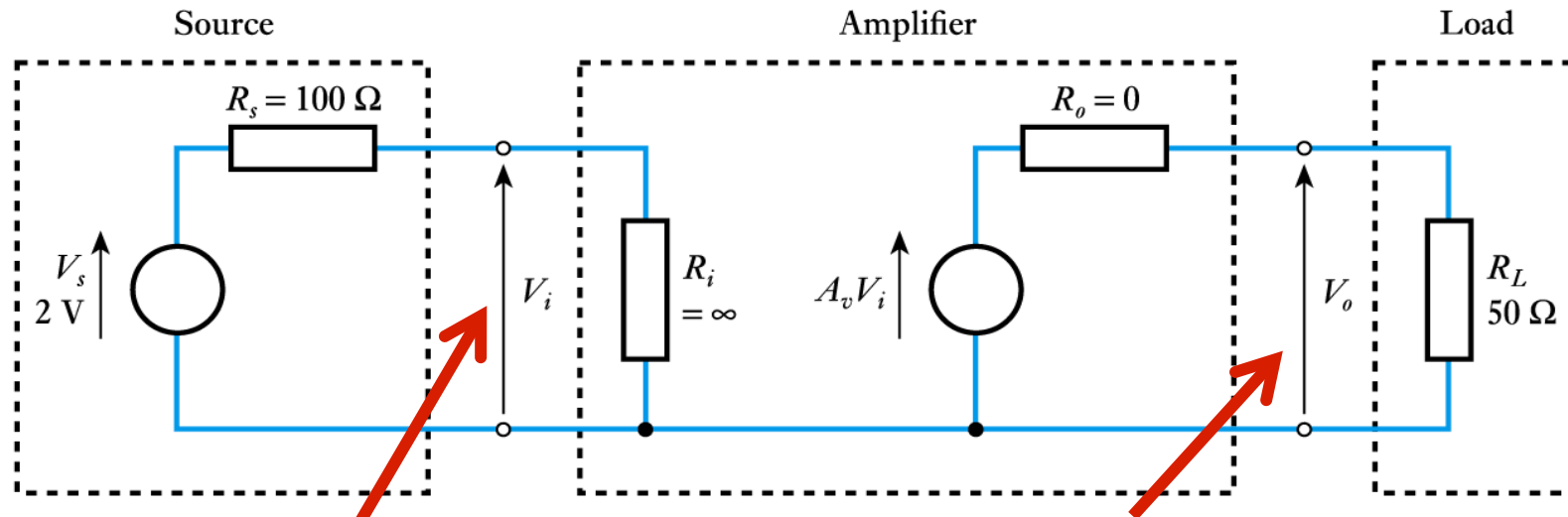
$$= 10 V_i \frac{50 \Omega}{10 \Omega + 50 \Omega}$$

$$= 10 \times 1.82 \frac{50 \Omega}{10 \Omega + 50 \Omega} = 15.2 \text{ V}$$

- ◆ The reduction of the voltage gain is due to **loading effects**.
- ◆ The original gain of the amplifier in isolation was 10. It is the **unloaded** gain.

# An ideal voltage amplifier

- ◆ An **ideal voltage amplifier** would not suffer from loading
  - it would have  $R_i = \infty$  and  $R_o = 0$



- ◆ If  $R_i = \infty$ , then

$$\frac{R_i}{R_s + R_i} \approx \frac{R_i}{R_i} = 1$$

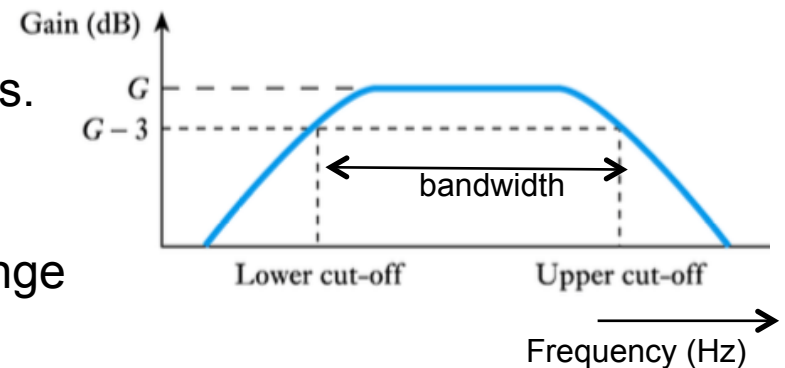
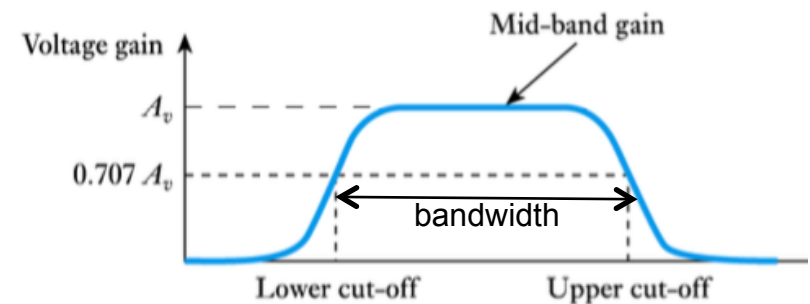
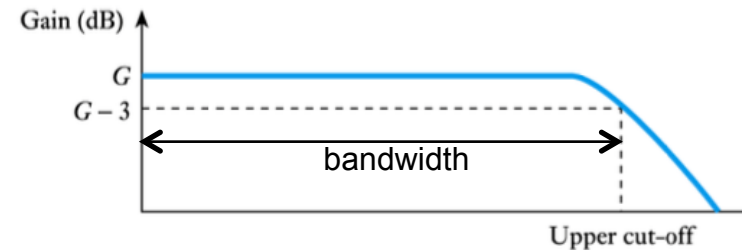
- ◆ and,

$$V_i = \frac{R_i}{R_s + R_i} V_s \approx V_s = 2\ \text{V}$$

$$\begin{aligned} V_o &= A_v V_i \frac{R_L}{R_o + R_L} \\ &= 10 V_i \frac{50\ \Omega}{0\ \Omega + 50\ \Omega} \\ &= 10 \times 2 \frac{50\ \Omega}{50\ \Omega} = 20\ \text{V} \end{aligned}$$

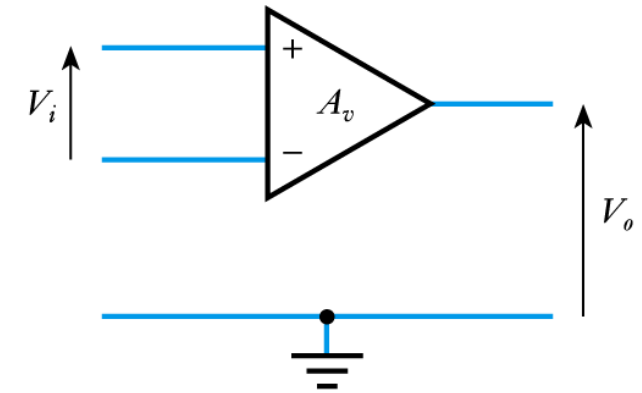
# Frequency response and bandwidth of Amplifier

- ◆ All real amplifiers have limits to the range of frequencies over which they can be used.
- ◆ The gain of a circuit in its normal operating range is termed its **mid-band gain**.
- ◆ The gain of all amplifiers falls at high frequencies.
  - Characteristic defined by the **half-power point**.
  - Gain falls to  $1/\sqrt{2} = 0.707$  (-3dB) times the mid-band gain.
  - This occurs at the **cut-off (or corner) frequency**.
- ◆ In some amplifiers gain also falls at low frequencies.
  - These are **AC coupled amplifiers**
- ◆ The **bandwidth** of the amplifier is the frequency range up to the -3dB point ( or cut-off frequencies)

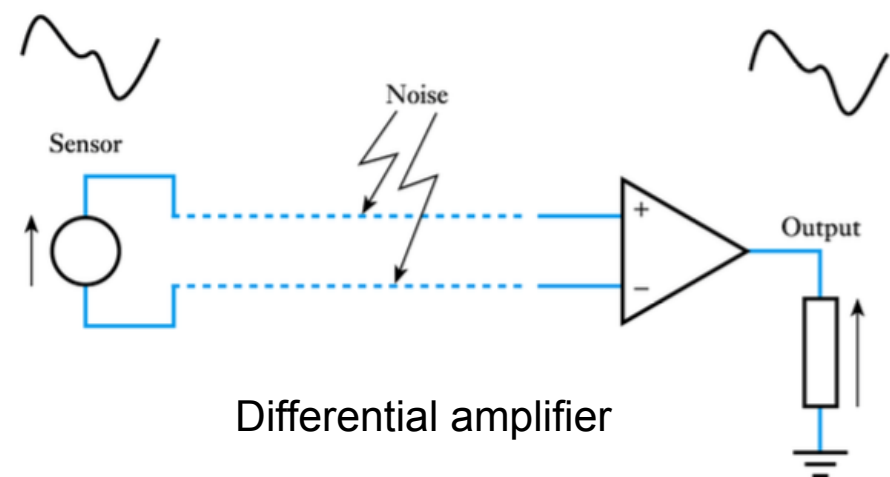
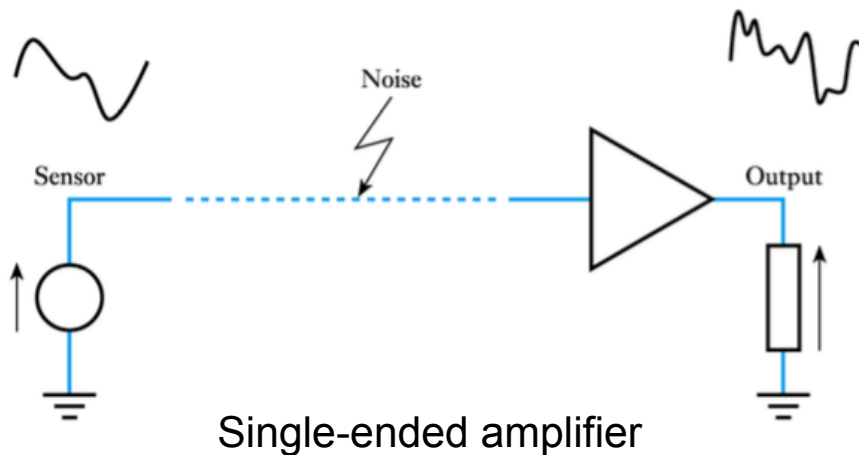


# Differential amplifiers

- ◆ Differential amplifiers have two inputs and amplify the voltage difference between them.
  - Inputs are called the **non-inverting input** (labelled +) and the **inverting input** (labelled -)



- ◆ An example of the use of a differential amplifier:



## Equivalent circuit of a differential amplifier

- ◆ In Lab 3, we will be using a common differential amplifier called **operational amplifier** (OpAmp).
- ◆ The equivalent circuit of such a differential amplifier is:

